

COMP2004 Programming Practice 2002 Summer School

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Assignment 3

- Paging simulation
- Background
- Your task
- Paging algorithms
 - First In First Out (FIFO)
 - Least Recently Used (LRU)
 - Pipelined LRU (PLRU)

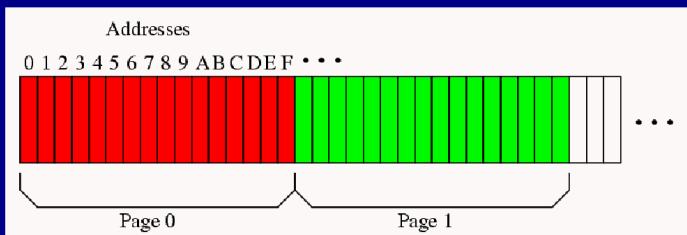
Background

- Read information from disk to memory as needed
 - Disk is slow
 - Memory is expensive

Addresses and pages

- Address
 - Specifies a byte on disk (≥ 0)
- Page
 - A block of bytes on disk
- Page number
 - Specifies a page on disk (≥ 0)
- Page size
 - Number of bytes per page
 - All pages have the same size

Pages diagram



- Each small box is a byte
 - Each has an address along the top
- A page is a block of bytes
 - Numbered from 0
- This diagram has a page size of 16

Finding page numbers

- For page size of 512 bytes:
 - Page 0 is addresses 0 to 511
 - Page 1 is addresses 512 to 1023
 - Page 2 is addresses 1024 to 1535
 - ...
- $\text{page number} = \text{address} / \text{page size}$
 - Using integer division
- Eg: page size of 4096, address 372921
 - $\text{Page number} = 372921 / 4096$
 $= 91.045166\dots$
 $= 91$

Frames

- Pages are read into **frames**
 - Pages are on disk
 - Frames are in memory
- A collection of frames is called a **cache**
 - Has only few frames
 - Compared to number of pages
 - ie. number of frames is limited
 - Stores only the pages needed right now

Cache diagram

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

- Each box is a frame
- Inside box:
 - Number indicating the page stored in that frame
 - r/w indicating frame clean/dirty
 - We'll get to this later

Accessing information

- As a program runs it needs to access data from disk
- Causes pages to be loaded into frames
- Program then accesses data in frame
- Entire page loaded into frame
- Each page present in at most one frame

Loading pages

- When a page is required, it may:
 - already be in a frame - **cache hit**
 - not be in a frame - **cache miss**
 - Requires page to be loaded into a frame before it can be used

Cache misses

- Initially all frames unused
 - Can load a page into any unused frame
- When all frames used
 - Must remove a frame before loading page
- **Paging algorithm**
 - Decides which frame to remove

Writing to frames

- Data access can be **read or write**
 - Read doesn't modify data value
 - Write may modify data value
- Writing causes data in frame to change
 - But not in page on disk
- Now data in frame and page differ
- Data in frame is more recent
- Frames in this state are **dirty**
- Frames identical to pages on disk are **clean**

Cache diagram revisited

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

- r indicates frame is clean
- w indicates frame is dirty

Write-back

- What happens if a dirty page is removed?
- Changes in frame must be put back to disk
 - This is called write-back
- Otherwise changes would be lost

Types of cache miss

- Cache miss causes frame to be removed
- Cache miss without write-back
 - Frame removed is clean
 - Unused frame available
- Cache miss with write-back
 - Frame removed is dirty

Your task

- Imagine a series of read/write operations
- Each results in one of
 - cache hit
 - cache miss without write-back
 - cache miss with write-back

Your code

- Is told about each operation in turn
- Simulates the paging algorithm
 - No need to actually read/write pages to/from disk/memory
 - Store which page is in each frame
 - And which frames are dirty
- Counts number of
 - cache hits
 - cache misses without write-back
 - cache misses with write-back

Classes

- Don't write a main() program
- One is supplied
 - Takes care of input/output
 - Calls methods in your class
 - Must be used
- Write the Cache and CacheFactory classes
 - Must be defined in Cache.h and CacheFactory.h files

Creating Cache objects

- How Cache objects are created is up to you
- Will be created with
- `string s; getline(cin, s);`
- `Cache *c = CacheFactory::createCache(s);`
- Takes a string, constructs an appropriate Cache object
- Returns a pointer to that newly constructed object

Creation string format

- Creation string is the first line read by the main program
- Has format:
 - F *page_size num_frames*
 - L *page_size num_frames*
 - P *page_size num_frames lookahead check_frames*
- *page_size, num_frames, lookahead, check_frames* are integers

Main loop

```
char mode;
Cache::addr_t address;
while (cin >> mode >> address) {
    if (mode == 'r') {
        c->read(address);
    } else if (mode == 'w') {
        c->write(address);
    }
    outputStats(*c);
}
```

Cache typedefs

- Various typedefs defined in the Cache class
- Each has an intended usage
- `Cache::addr_t`
 - Stores an address
- `Cache::page_t`
 - Stores a page number
- `Cache::counter_t`
 - Stores a counter
 - eg. num of cache hits, etc

Output

```
void outputStats(const Cache &c) {
    Cache::counter_t hits = c.getHits(),
                    misses = c.getMisses(),
                    missesWB = c.getMissesWB();

    cout << hits << " " <<
                    misses << " " <<
                    missesWB << endl;
}
```

- Performed after every read/write operation and at end of program

Paging algorithms

- First In First Out (FIFO)
- Least Recently Used (LRU)
- Pipelined LRU (PLRU)
- This order is easiest to hardest
- For automarking:
 - FIFO : 40%
 - LRU : 40%
 - PLRU : 20%

First In First Out (FIFO)

- Very simple
- Remove frame which has been in the cache for the longest time
- Can think of the cache as a list/queue
 - New frames go at front
 - Old frames removed from back
- Don't have to store it as a list/queue
 - Can store however you like
 - Choose an efficient method

FIFO Example

- num_frames = 6, page_size = 512
- w 2000 (page 3)
- w 1492 (page 2)

Initially:

5 r	1 r	42 r	30 w	4 r	3 r
--------	--------	---------	---------	--------	--------

Read: w 2000

5 r	1 r	42 r	30 w	4 r	3 w
--------	--------	---------	---------	--------	--------

 Cache Hit

Read: w 1492

2 w	5 r	1 r	42 r	30 w	4 r
--------	--------	--------	---------	---------	--------

 Cache Miss With Write-back

Least Recently Used (LRU)

- Improves on FIFO
- When a frame is accessed (cache hit)
 - Moved to the front of the list/queue
- Now recently used frames are at front
- Frames not recently used are at back
- Still removes frame from back
 - The least recently used frame

LRU Example

- num_frames = 6, page_size = 512
- w 2000 (page 3)
- w 1492 (page 2)

Initially:

5 r	1 r	42 r	30 w	4 r	3 r
--------	--------	---------	---------	--------	--------

Read: w 2000

3 w	5 r	1 r	42 r	30 w	4 r
--------	--------	--------	---------	---------	--------

 Cache Hit

Read: w 1492

2 w	3 w	5 r	1 r	42 r	30 w
--------	--------	--------	--------	---------	---------

 Cache Miss Without Write-back

Pipelined LRU (PLRU)

- Hardest/most complex
 - Worth less than FIFO and LRU
 - Therefore attack it last
 - Don't let it ruin your design
- Improves on LRU
- Doesn't remove frames which will be needed soon
- Achieves this by examining the upcoming read/write operations

Pipelining and lookahead list

- Lookahead list is a list of upcoming read/write operations
- Has max length given by *lookahead*
- Best way to understand is with an example
 - Lookahead list length will be 4
 - Lookahead list shown in yellow
 - * indicates current input position
 - + indicates operation just processed

Lookahead list example

w 2000 Contains 0 operations.
w 1492 0 operations processed.
r 456 Initially empty.
w 24121
r 24120
r 34
r 4592
r 2000
w 2000
r 1492
r 24120

Lookahead list example

* w 2000 Contains 1 operation.
w 1492 0 operations processed.
r 456
w 24121
r 24120
r 34
r 4592
r 2000
w 2000
r 1492
r 24120

Lookahead list example

w 2000 Contains 2 operations.
* w 1492 0 operations processed.
r 456
w 24121
r 24120
r 34
r 4592
r 2000
w 2000
r 1492
r 24120

Lookahead list example

w 2000 Contains 3 operations.
w 1492 0 operations processed.
* r 456
w 24121
r 24120
r 34
r 4592
r 2000
w 2000
r 1492
r 24120

Lookahead list example

w 2000 Contains 4 operations.
w 1492 0 operations processed.
r 456
* w 24121
r 24120
r 34
r 4592
r 2000
w 2000
r 1492
r 24120

Lookahead list example

+ w 2000 Contains 4 operations.
w 1492 1 operation processed.
r 456
w 24121
* r 24120
r 34
r 4592
r 2000
w 2000
r 1492
r 24120

Lookahead list example

```
w 2000    Contains 4 operations.  
+ w 1492    2 operations processed.  
  r 456  
  w 24121  
  r 24120  
* r 34  
  r 4592  
  r 2000  
w 2000  
r 1492  
r 24120
```

Lookahead list example

```
w 2000    Contains 4 operations.  
w 1492    3 operations processed.  
+ r 456  
  w 24121  
  r 24120  
  r 34  
* r 4592  
  r 2000  
w 2000  
r 1492  
r 24120
```

Lookahead list example

```
w 2000    Contains 4 operations.  
w 1492    4 operations processed.  
r 456  
+ w 24121  
  r 24120  
  r 34  
  r 4592  
* r 2000  
w 2000  
r 1492  
r 24120
```

Lookahead list example

```
w 2000    Contains 4 operations.  
w 1492    5 operations processed.  
r 456  
w 24121  
+ r 24120  
  r 34  
  r 4592  
  r 2000  
* w 2000  
  r 1492  
  r 24120
```

Lookahead list example

```
w 2000    Contains 4 operations.  
w 1492    6 operations processed.  
r 456  
w 24121  
r 24120  
+ r 34  
  r 4592  
  r 2000  
w 2000  
* r 1492  
  r 24120
```

Lookahead list example

```
w 2000    Contains 4 operations.  
w 1492    7 operations processed.  
r 456  
w 24121  
r 24120  
r 34  
+ r 4592  
  r 2000  
w 2000  
r 1492  
* r 24120
```

Lookahead list example

```
w 2000 Contains 4 operations.  
w 1492 7 operations processed.  
r 456  
w 24121 No more input!  
r 24120 flush() is called, which  
r 34 indicates to process the  
+ r 4592 rest of the lookahead list.  
r 2000  
w 2000  
r 1492  
* r 24120
```

Lookahead list example

```
w 2000 Contains 3 operations.  
w 1492 8 operations processed.  
r 456  
w 24121  
r 24120  
r 34  
r 4592  
+ r 2000  
w 2000  
r 1492  
r 24120
```

Lookahead list example

```
w 2000 Contains 2 operations.  
w 1492 9 operations processed.  
r 456  
w 24121  
r 24120  
r 34  
r 4592  
r 2000  
+ w 2000  
r 1492  
r 24120
```

Lookahead list example

```
w 2000 Contains 1 operation.  
w 1492 10 operations processed.  
r 456  
w 24121  
r 24120  
r 34  
r 4592  
r 2000  
w 2000  
+ r 1492  
r 24120
```

Lookahead list example

```
w 2000 Contains 0 operations.  
w 1492 All 11 operations  
r 456 processed.  
w 24121  
r 24120  
r 34  
r 4592  
r 2000  
w 2000  
r 1492  
+ r 24120
```

Finding frame to remove

- Starts from back of cache list
- Examines frames one at a time
- When it finds one which isn't needed by the operations in the lookahead list
 - This is the frame which is removed
- Examines at most **check_frames** frames

PLRU example 1

- num_frames = 6, page_size = 512
- lookahead = 3, check_frames = 4
- Current operation:
 - w 1492 (page 2)
- Lookahead list:
 - w 50 (page 0)
 - w 15400 (page 30)
 - r 2200 (page 4)

PLRU example 1

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

- Page 2 is not in cache
- Cache miss
- Must find a frame to remove

PLRU example 1

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

v

^

- Start at back of list
- Page 4 is in lookahead list
- Don't remove this frame
- Normal LRU algorithm would blindly remove this frame

PLRU example 1

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

v

^

- Move to next frame
- Page 30 is in lookahead list
- Don't remove this frame

PLRU example 1

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

v

^

- Move to next frame
- Page 42 is NOT in lookahead list
- Remove this frame
- Then add page 2 as usual

PLRU example 1

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

Finally:

2	3	5	1	30	4
w	w	r	r	w	r

- Pages 30 and 4 are still in cache
- So will be cache hits when the upcoming operations are processed

All frames needed soon?

- What if we examine all *check_frames* frames and all are in lookahead list?
- Which one do we choose to remove?
- The one which is first needed at the latest time
 - An example should make it clear

All frames needed example

```
w 1492 (page 2)
w 50 (page 0)
w 15400 (page 30)
w 15300 (page 30)
w 180 (page 0)
r 2200 (page 4)
w 1292 (page 2)
```

- Consider this lookahead list
- Suppose all checked frames are in this lookahead list
 - Which frame do we remove?

All frames needed example

```
w 1492 (page 2)
w 50 (page 0)
w 15400 (page 30)
w 15300 (page 30)
w 180 (page 0)
r 2200 (page 4)
w 1292 (page 2)
```

All frames needed example

```
w 1492 (page 2) First (page 2)
w 50 (page 0)
w 15400 (page 30)
w 15300 (page 30)
w 180 (page 0)
r 2200 (page 4)
w 1292 (page 2)
```

All frames needed example

```
w 1492 (page 2) First (page 2)
w 50 (page 0) First (page 0)
w 15400 (page 30)
w 15300 (page 30)
w 180 (page 0)
r 2200 (page 4)
w 1292 (page 2)
```

All frames needed example

```
w 1492 (page 2) First (page 2)
w 50 (page 0) First (page 0)
w 15400 (page 30) First (page 30)
w 15300 (page 30)
w 180 (page 0)
r 2200 (page 4)
w 1292 (page 2)
```

All frames needed example

```
w 1492 (page 2) First (page 2)
w 50 (page 0) First (page 0)
w 15400 (page 30) First (page 30)
w 15300 (page 30)
w 180 (page 0)
r 2200 (page 4) First (page 4)
w 1292 (page 2)
```

All frames needed example

```
w 1492 (page 2) First (page 2)
w 50 (page 0) First (page 0)
w 15400 (page 30) First (page 30)
w 15300 (page 30)
w 180 (page 0)
r 2200 (page 4) First (page 4)
w 1292 (page 2)
```

- Construct a list in order of when pages are first used, ie: 2, 0, 30, 4
 - Use the last item, ie. remove frame containing page 4

PLRU example 2

- Same as before, except:
 - check_frames = 2
- num_frames = 6, page_size = 512
- lookahead = 3, check_frames = 2
- Current operation:
 - w 1492 (page 2)
- Lookahead list:
 - w 50 (page 0)
 - w 15400 (page 30)
 - r 2200 (page 4)

PLRU example 2

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

- Page 2 is not in cache
- Cache miss
- Must find a frame to remove

PLRU example 2

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

v

^

- Start at back of list
- Page 4 is in lookahead list
- Don't remove this frame

PLRU example 2

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

v

^

- Move to next frame
- Page 30 is in lookahead list
- Don't remove this frame

PLRU example 2

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

^ ^

- Cannot move to next frame
 - Since *check_frames* is only 2
- Must choose one of the last 2 frames

PLRU example 2

- Examine lookahead list:

- w 50 (page 0)
- w 15400 (page 30)
- r 2200 (page 4)

- Page 30 is needed before page 4
- So remove page 4

PLRU example 2

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

Finally:

2	3	5	1	42	30
w	w	r	r	r	w

- Same as normal LRU
- We were unlucky

PLRU example 3

- What if the page 30 and page 4 operations were swapped?

- w 50 (page 0)
- r 2200 (page 4)
- w 15400 (page 30)

^ ^

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

^ ^

- Still must choose one of last 2 frames

PLRU example 3

- This time page 4 is needed before page 30
- So remove page 30

Initially:

3	5	1	42	30	4
w	r	r	r	w	r

Finally:

2	3	5	1	42	4
w	w	r	r	r	r